Mathematical Analysis of a PDE System modeling biological Network Formation

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We present an analysis of a parabolic-elliptic PDE system modeling the formation of biological networks. The unknowns are the network pressure (satisfying a Darcy-type law) and the nework conductance. We discuss existence of weak and strong time dependent solutions, stability and instability of steady states and pattern formation in the small diffusion limit.